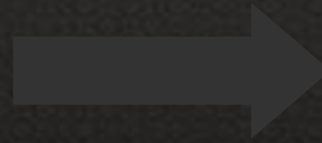


# Quantifying Long-Term Scientific Impact

Scientific Impact



Citations

## Citation-based measures:

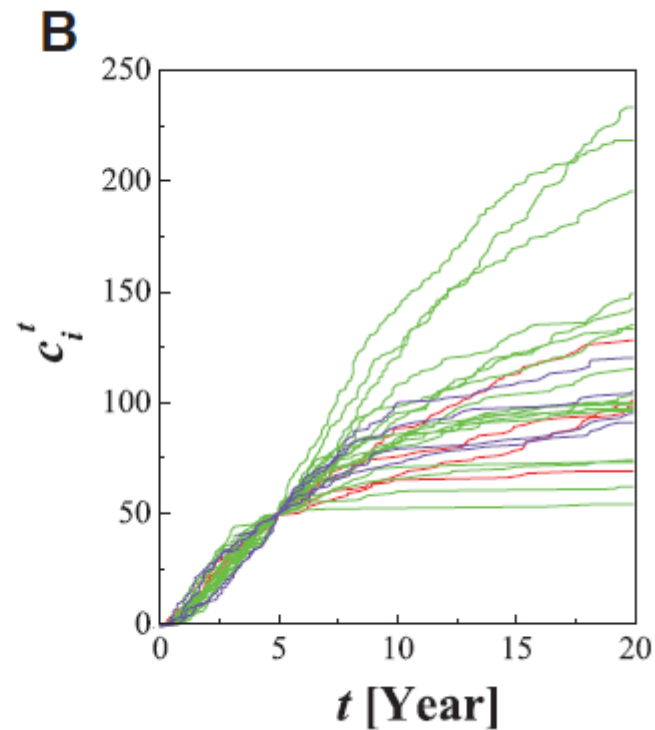
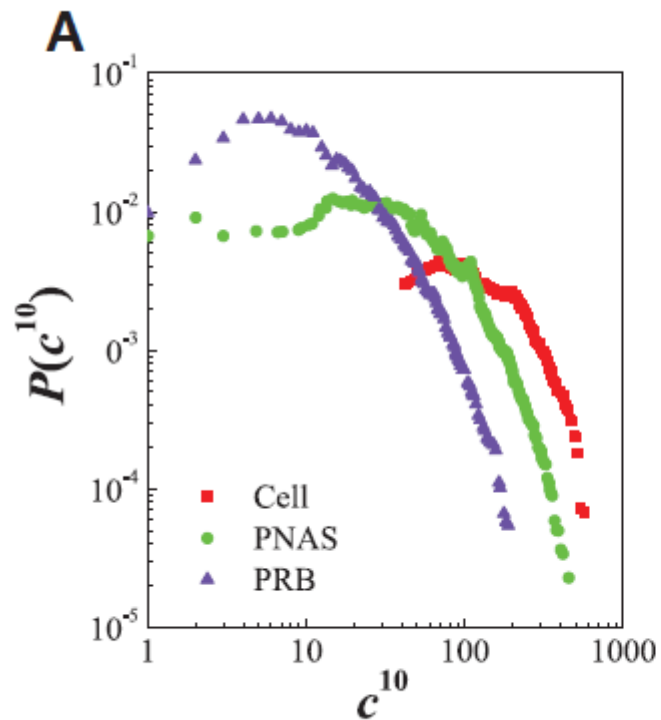
- Impact factor (IF)
- The number of citations
- Hirsch index
- Others

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Citation-based measures lack  
long-term predictability

Papers published in the same journal a decade later acquire widely different number of citations, from one to thousands

A group of papers that within a 5-year span collect the same number of citations are found to have widely different long-term impacts



- Citation distributions
- Rescale discipline-dependent variables

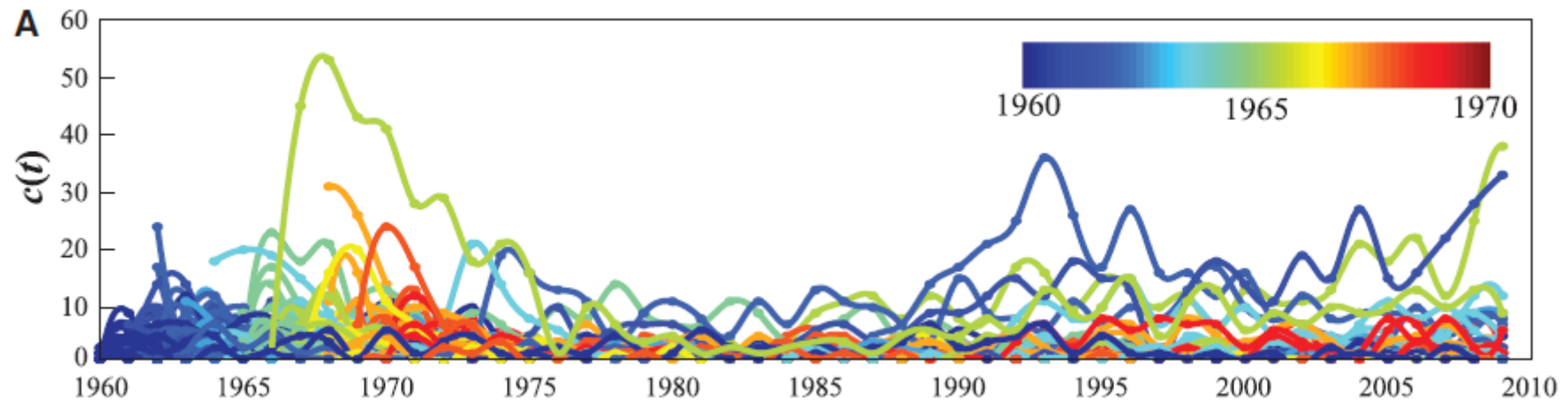


Aggregated citation patterns are characterized by generic scaling laws

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Little is known about the mechanisms governing the citation histories of individual papers

Randomly select 200 papers published  
between 1960 and 1970 in the  
(Physical Review) PR corpus.



- Lack of order
- Hence lack of predictability



This lack of order in citation histories is only apparent, because citations follow widely reproducible dynamical patterns that span research fields.

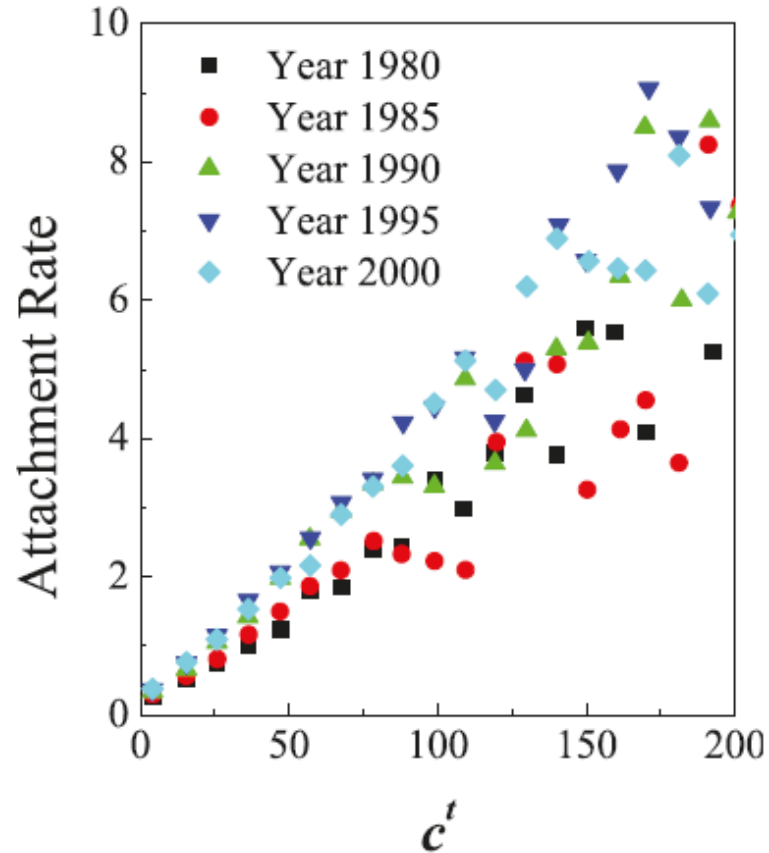
Three fundamental mechanisms that drive the citation history of individual papers:

■ Preferential attachment

■ Aging

■ Fitness

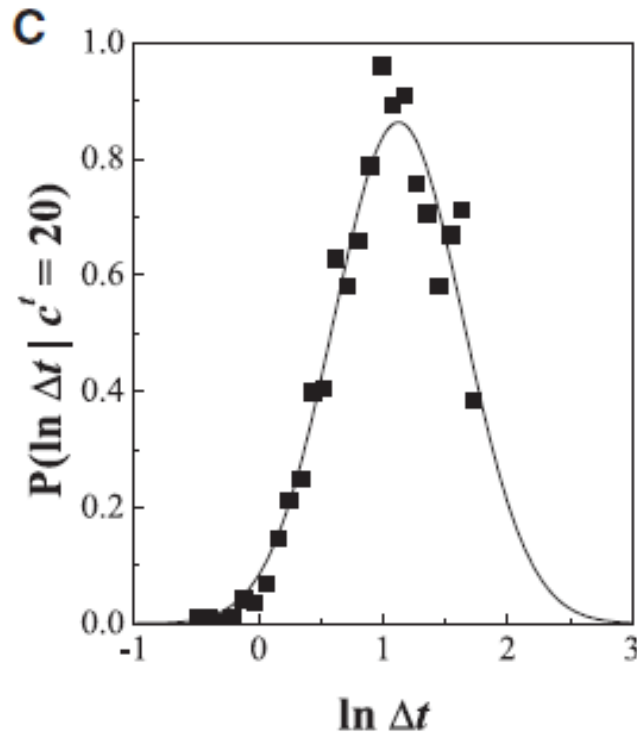
# Preferential Attachment



$c_i^t$ : the citations of each paper before this year



# Aging



$$P(\Delta t) = \frac{1}{\sqrt{2\pi}\sigma\Delta t} \exp\left(-\frac{(\ln \Delta t - \mu)^2}{2\sigma^2}\right).$$

$\mu$  governs the time for a paper to reach its citation peak

$\sigma$  captures the decay rate

$P_i(t)$ : log-normal survival probability

# Fitness

Inherent differences between papers  
novelty and importance of a discovery



$\eta_i$ : the community's response to a work.

The probability that paper  $i$  is cited at time  $t$  after publication

$$\Pi_i(t) \sim \eta_i c_i^t P_i(t)$$


$$\Delta t_i = t - t_i = \beta^{-1} \ln(N/i),$$

$$c_i^t = m \left( e^{\lambda_i \Phi\left(\frac{\ln t - \mu_i}{\sigma_i}\right)} - 1 \right).$$

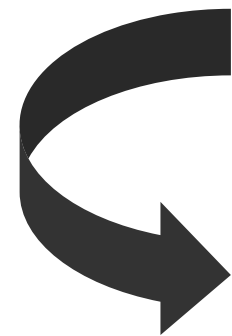
$$\Phi(x) \equiv (2\pi)^{-1/2} \int_{-\infty}^x e^{-y^2/2} dy. \quad \lambda_i \equiv \eta_i \beta / A$$

- $m$ : the average number of references each new paper contains
- $\beta$ : the growth rate of the total number of publications
- $A$ : is a normalization constant

$$c_i^t = m \left( e^{\lambda_i \Phi \left( \frac{\ln t - \mu_i}{\sigma_i} \right)} - 1 \right).$$


$$t \rightarrow \infty \quad c_i^t \rightarrow c_i^\infty \quad \varphi \rightarrow 1$$
$$c_i^\infty = m \left( e^{\lambda_i} - 1 \right)$$

The ultimate impact of a paper is only determined by the relative fitness.



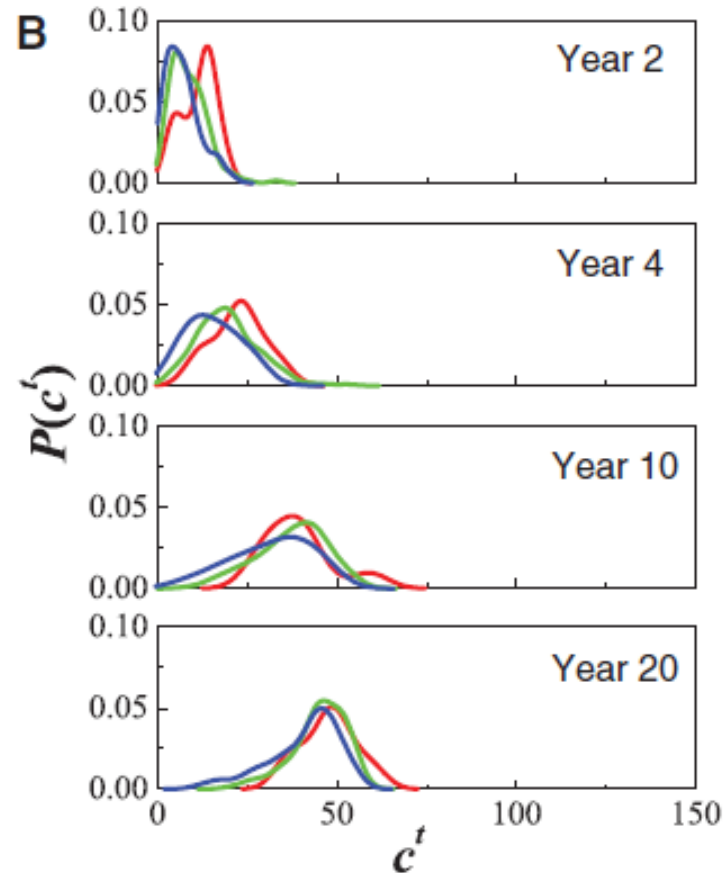
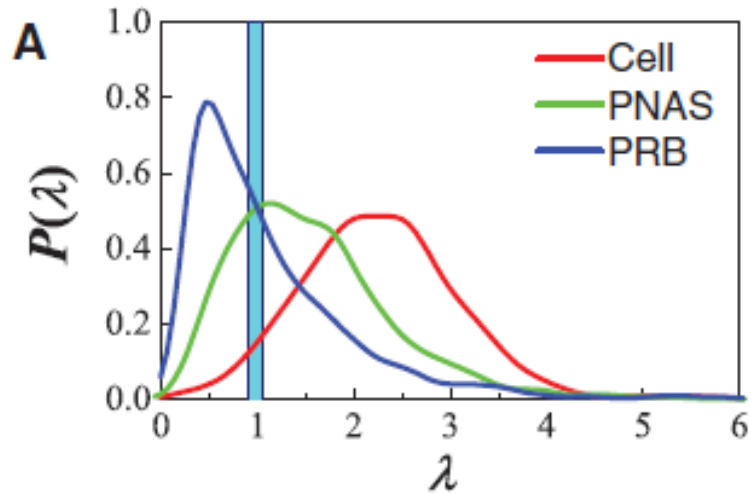
$$T_i^* \approx \exp(\mu_i).$$

The impact time is mainly determined by  $\mu_i$

The proposed model offers a journal-free methodology to evaluate long term impact.

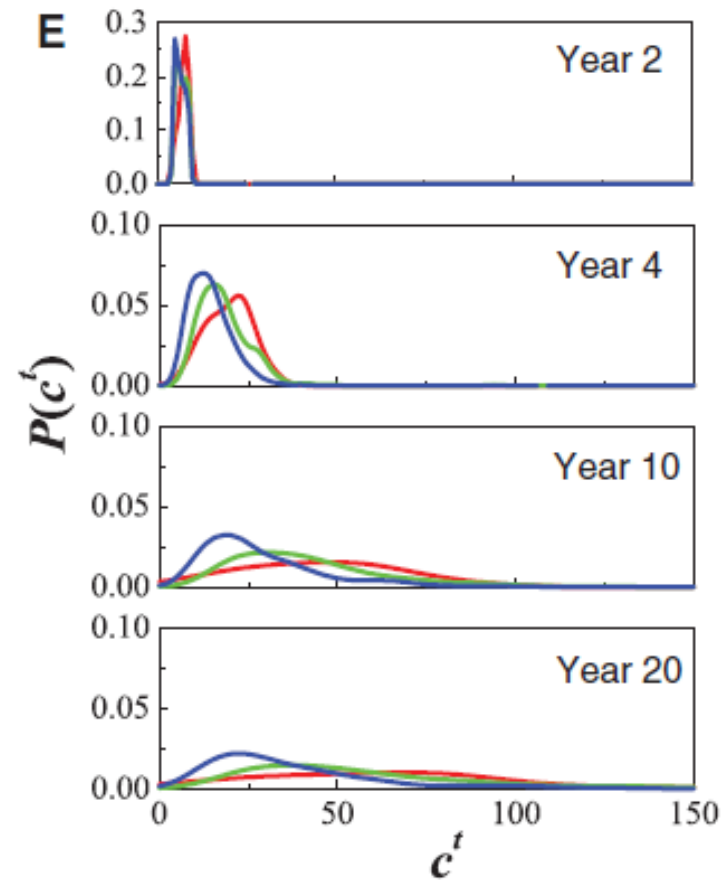
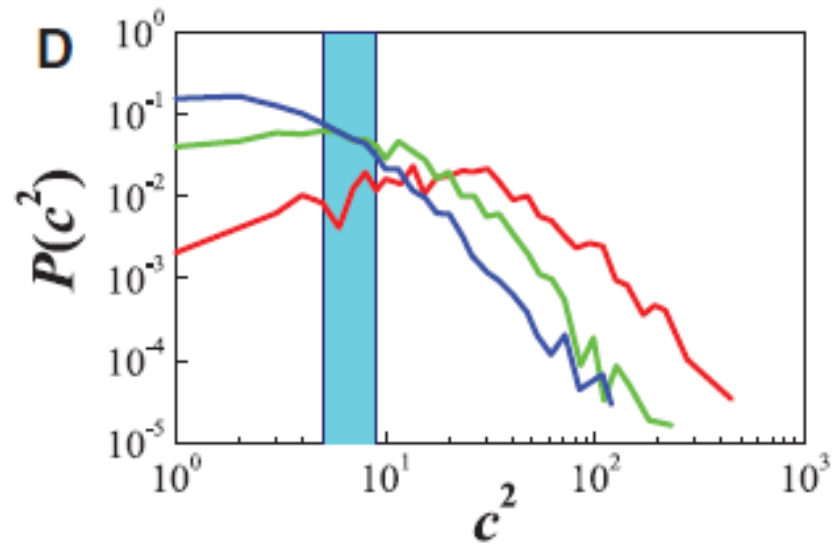
Journal	IF
<i>Physical Review B (PRB)</i>	3.26
<i>Proceedings of the National Academy of Sciences USA (PNAS)</i>	10.48
<i>Cell</i>	33.62

# Fitness Selection



Convergence

# Citation & IF Selection

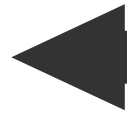


Diverge



# Calculating the IF

$\Lambda M \Sigma$



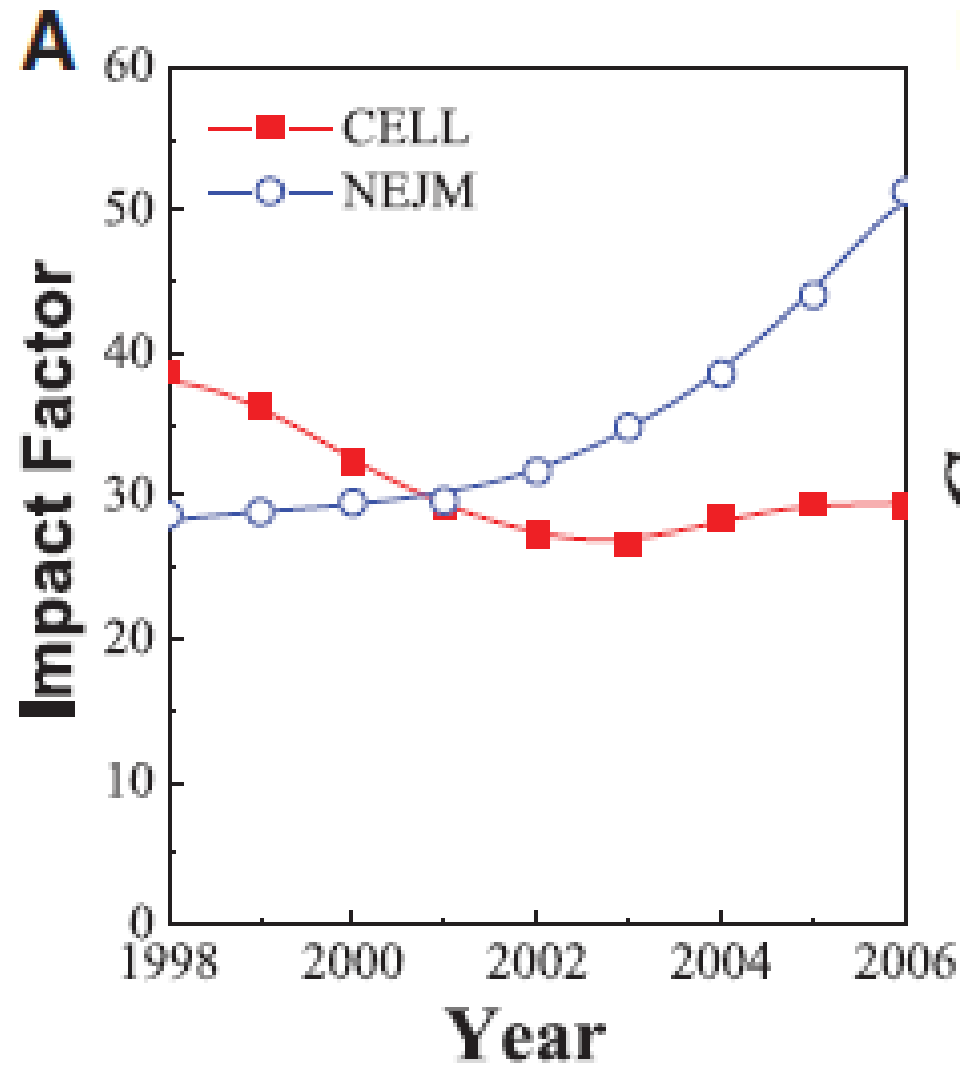
$\lambda \mu \sigma$

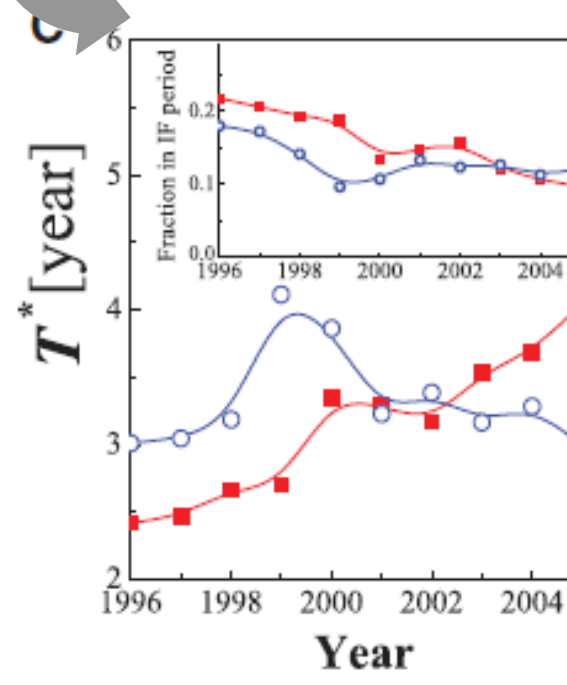
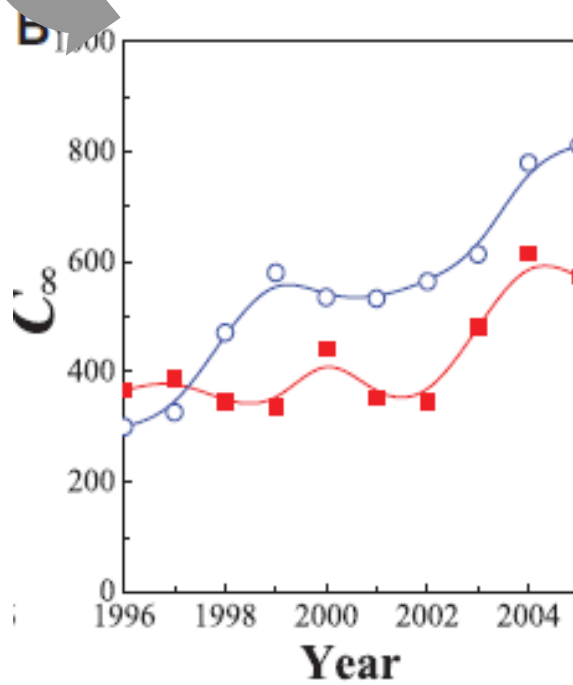
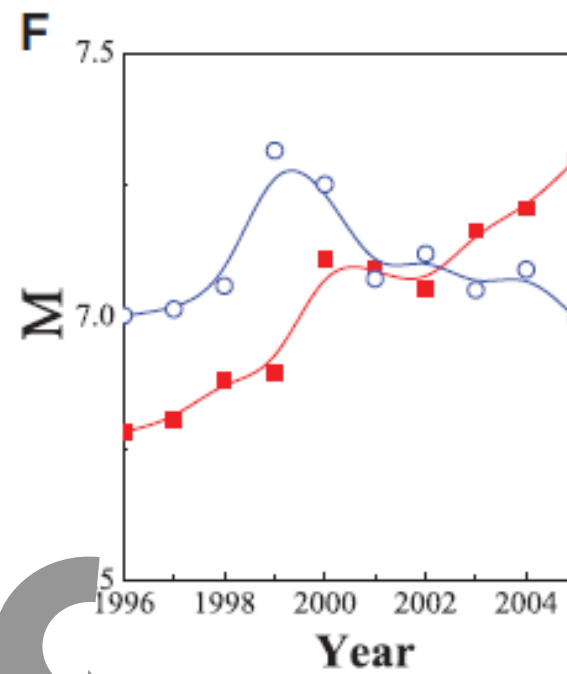
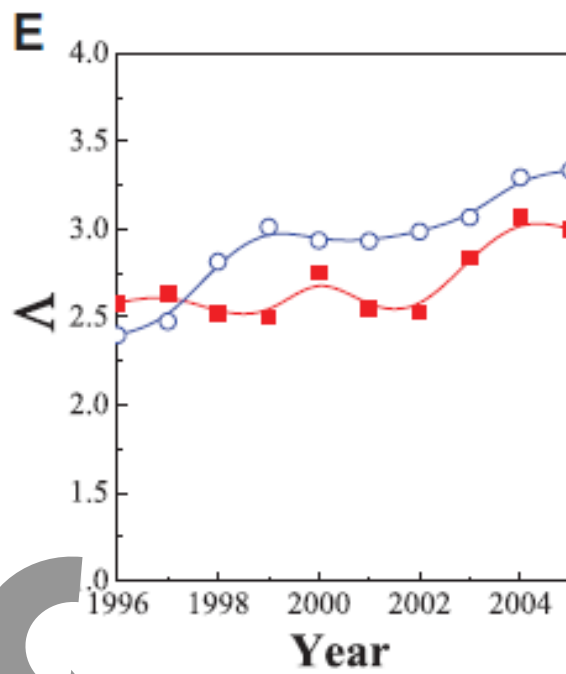
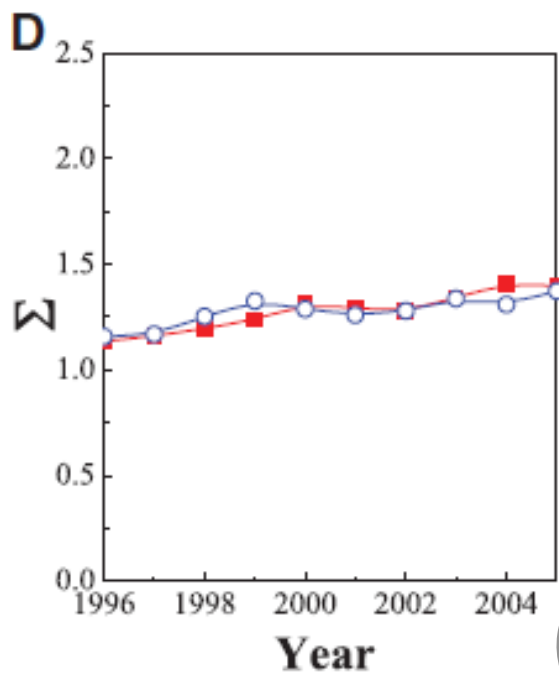
$$\text{IF} \approx \frac{m}{2} \left( \exp \left[ \Lambda \Phi \left( \frac{M_1 - M}{\Sigma} \right) \right] - \exp \left[ \Lambda \Phi \left( \frac{M_2 - M}{\Sigma} \right) \right] \right).$$

$$C^{\text{top}} = m(e^{\Lambda} - 1).$$

$$T^* = \exp(M)$$

# Illustrate the changes of IF





# Predict future citations

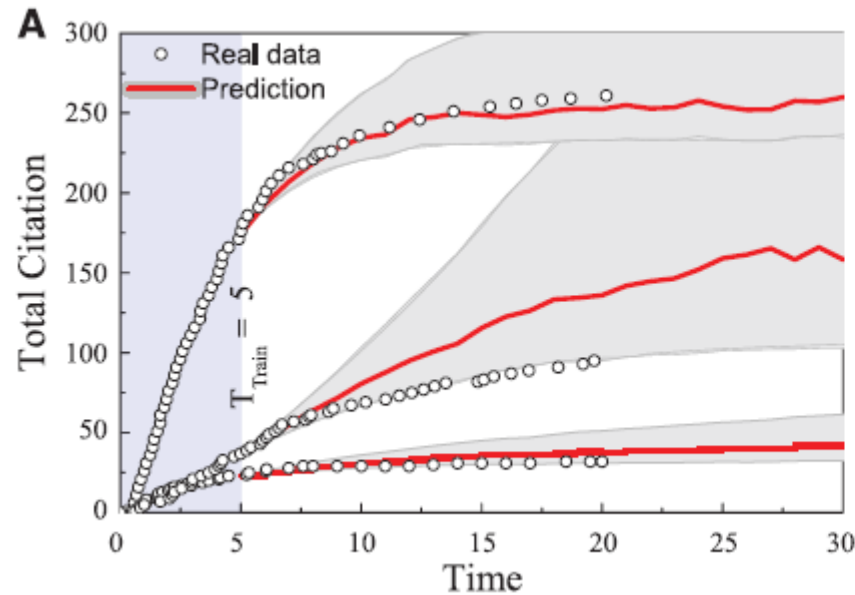
$$\sigma_p^+ = \sqrt{\int_{k_p^*}^{\infty} (k_p - k_p^*)^2 P(k_p) dk_p}$$

$$\sigma_p^- = \sqrt{\int_{k_t}^{k_p^*} (k_p - k_p^*)^2 P(k_p) dk_p}$$

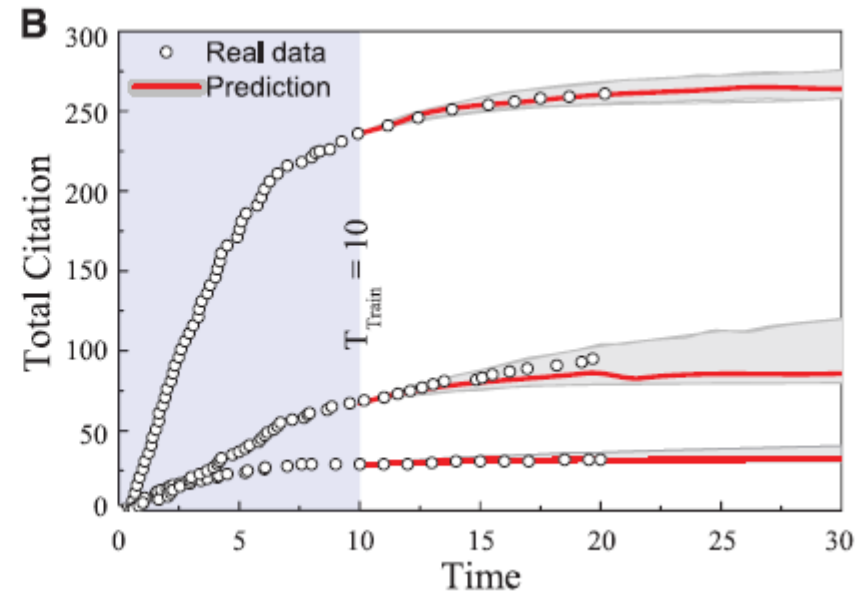
citation envelope

$$[-\sigma_p^-, \sigma_p^+]$$

5 years  $T_{\text{train}}$



10 years  $T_{\text{train}}$



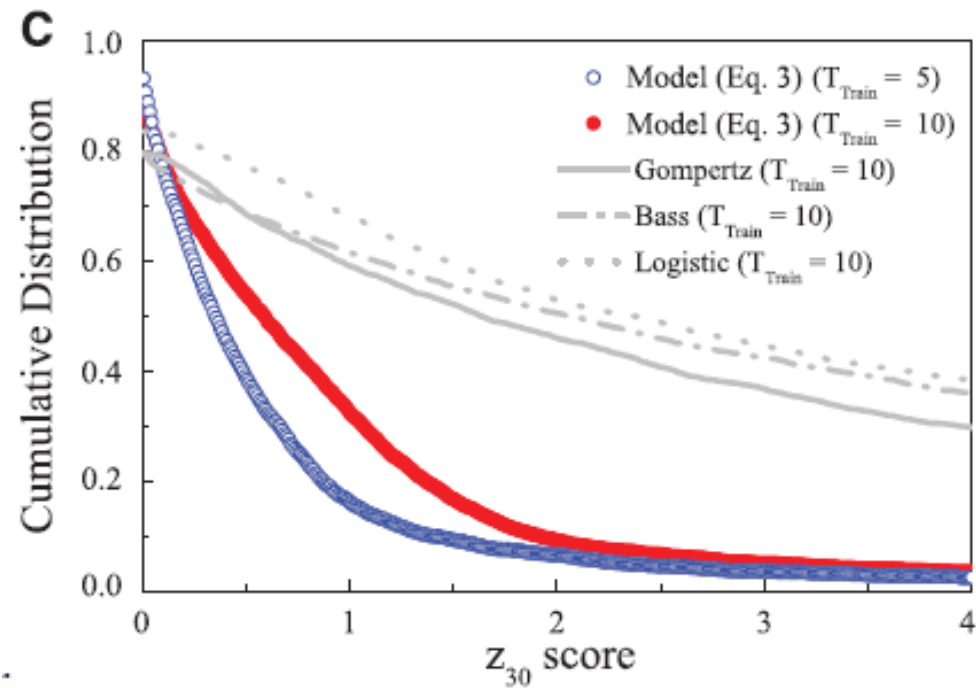
# Our Model

## Logistic Model

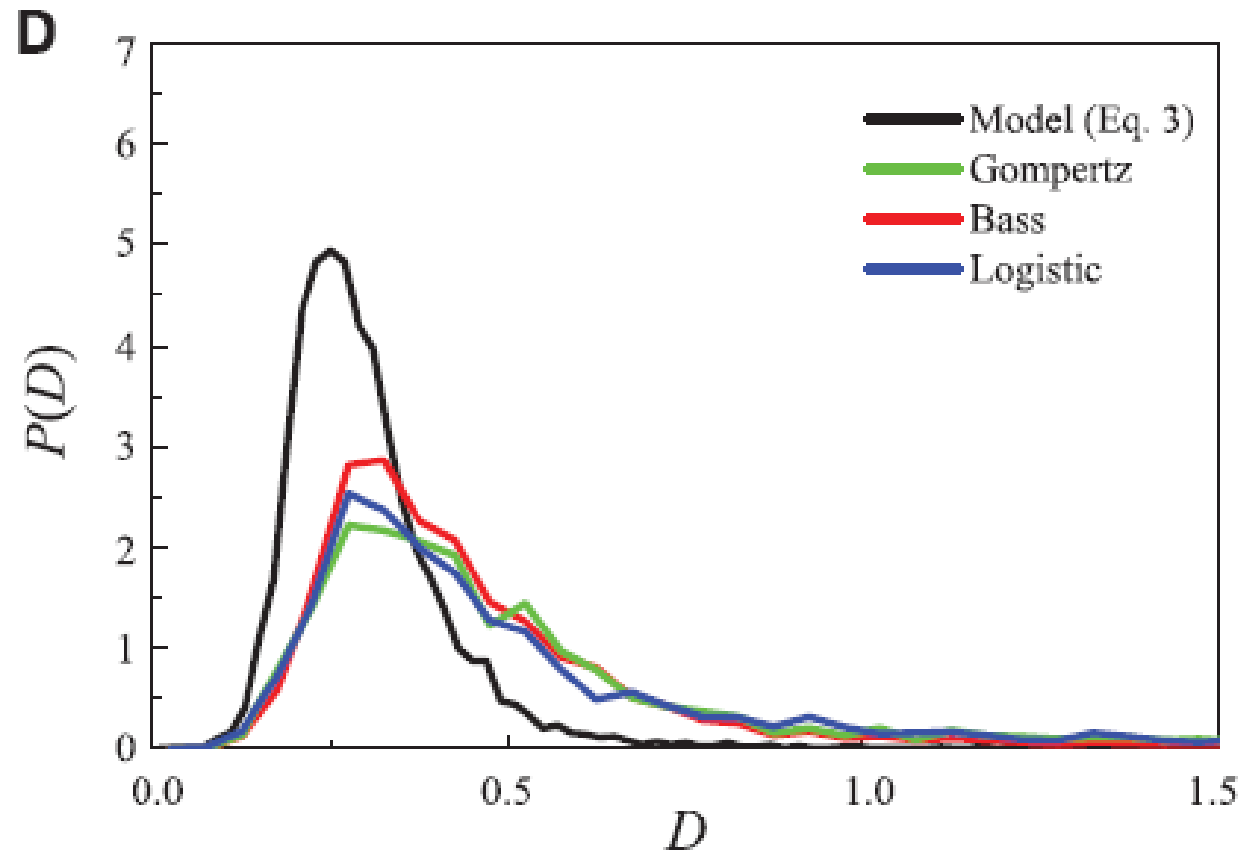
## Bass Model

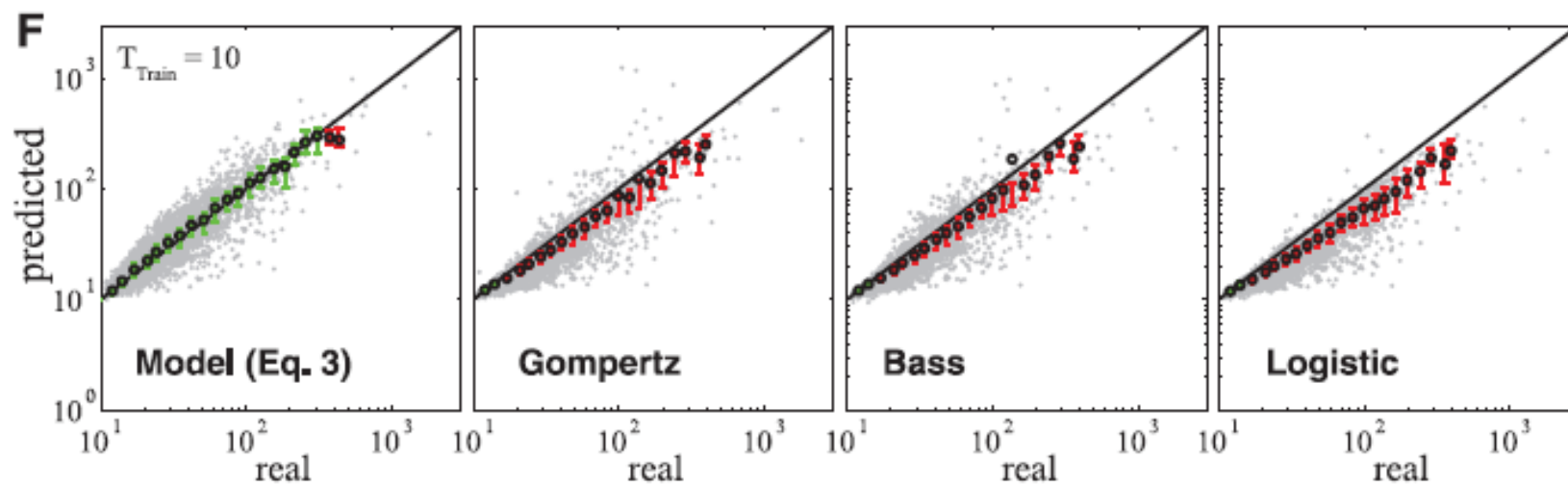
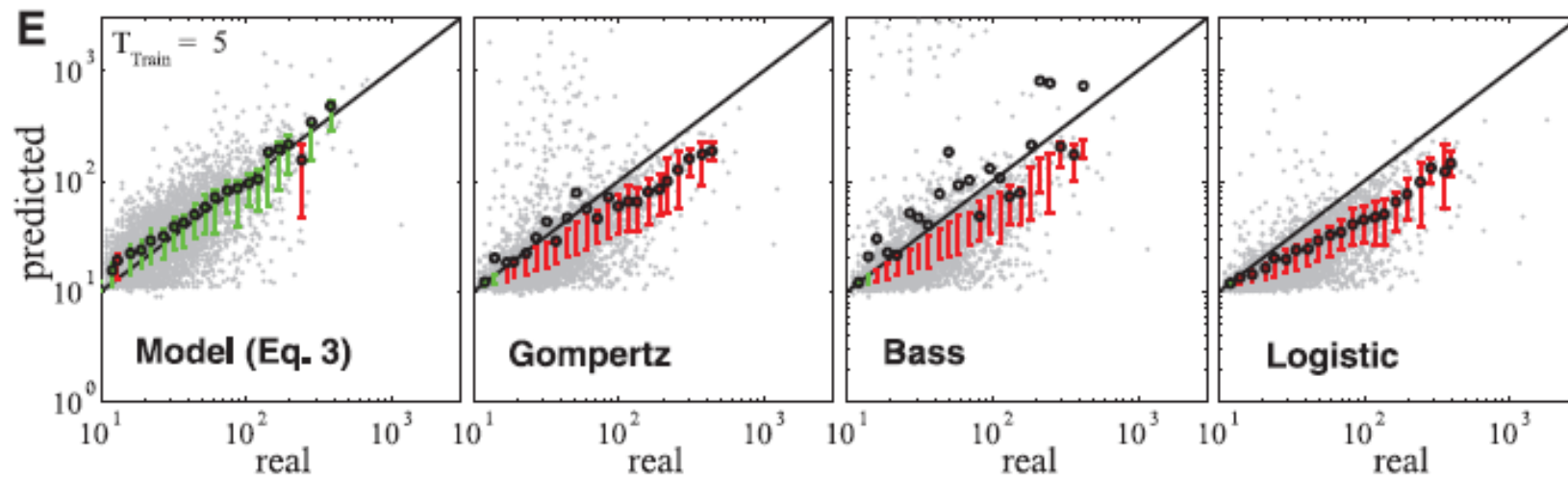
## Gompertz Model

$$z_T = |c^T - k_p^*| / \sigma_p^+$$



# Kolmogorov-Smirnov (KS) test





# Limitations

- It cannot account for exogenous “second acts,” like the citation bump observed for superconductivity papers after the discovery of high-temperature superconductivity in the 1980s,
- It cannot detect delayed impact, like the explosion of citations to Erdős and Rényi’s work 4 decades after their publication, following the emergence of network science



Thank you for listening!